

N94-18554

59-34

186471

P-14

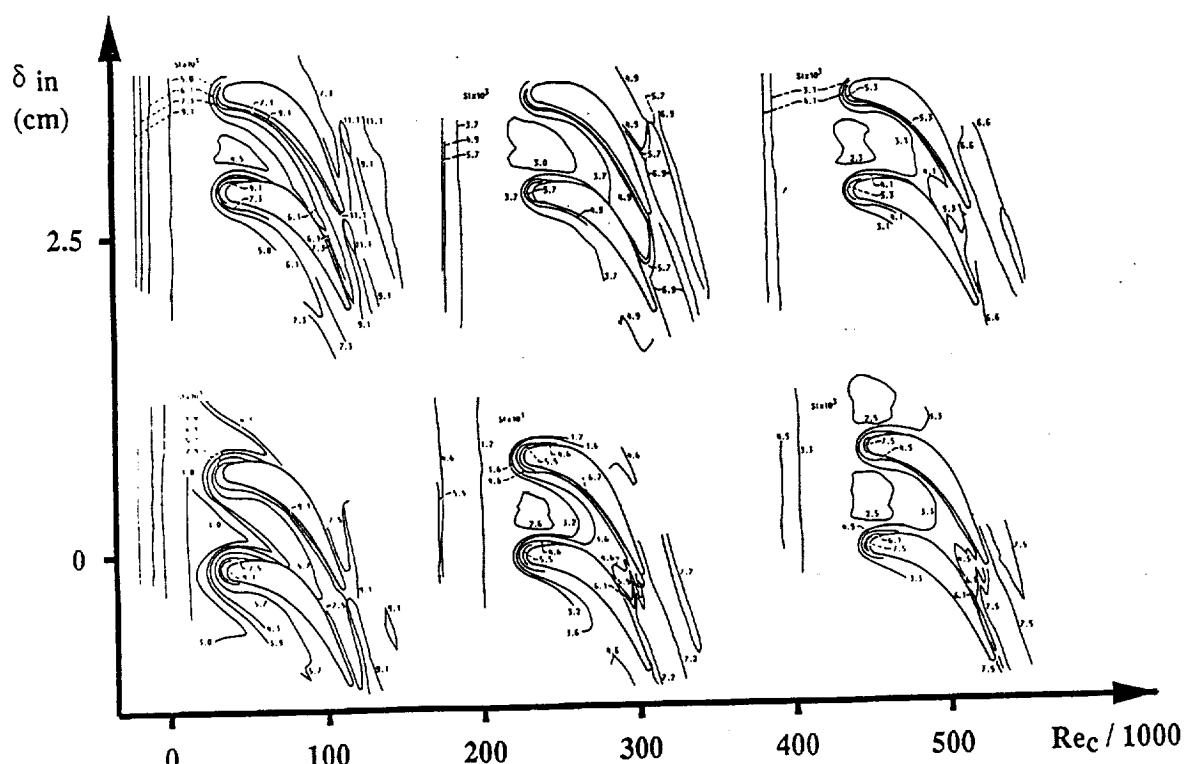
AN ALGEBRAIC TURBULENCE MODEL
FOR TURBOMACHINERY

by

Rodrick V. Chima
NASA Lewis Research Center
Cleveland, Ohio

OVERVIEW

- MOTIVATION - TURBINE ENDWALL HEAT TRANSFER
- DESCRIPTION OF NEW MODEL
- RESULTS
 - 1. FLAT PLATE
 - 2. ANNULAR TURBINE CASCADE
 - 3. TURBINE ENDWALL HEAT TRANSFER
 - 4. SUPERSONIC COMPRESSOR BLADE
- SUMMARY



EXPERIMENTAL ENDWALL STANTON NUMBER CONTOURS

AS A FUNCTION OF δ_{inlet} AND Re_{chord}

RVC3D (ROTOR VISCOUS CODE 3-D)

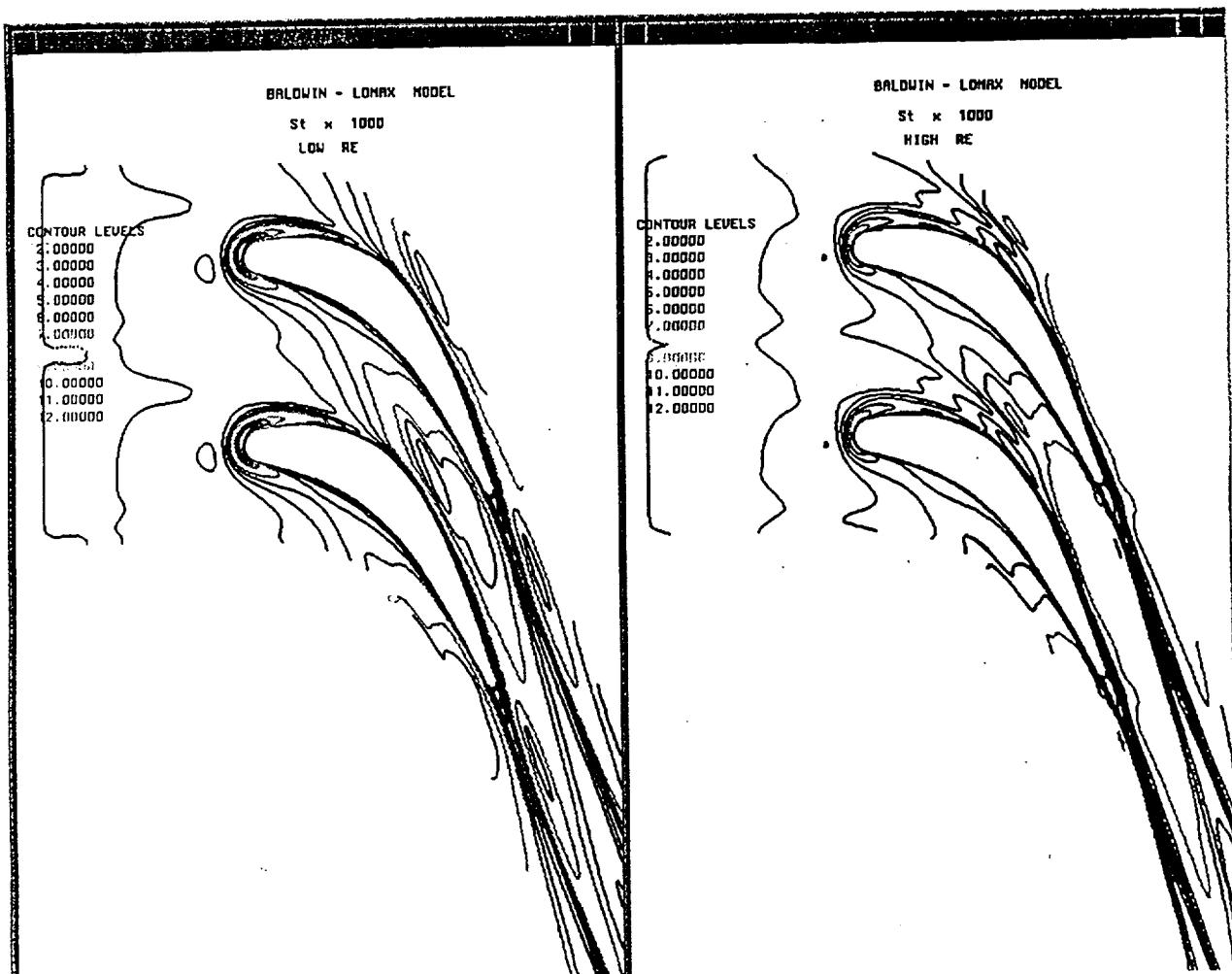
BY R. V. CHIMA

DESCRIPTION

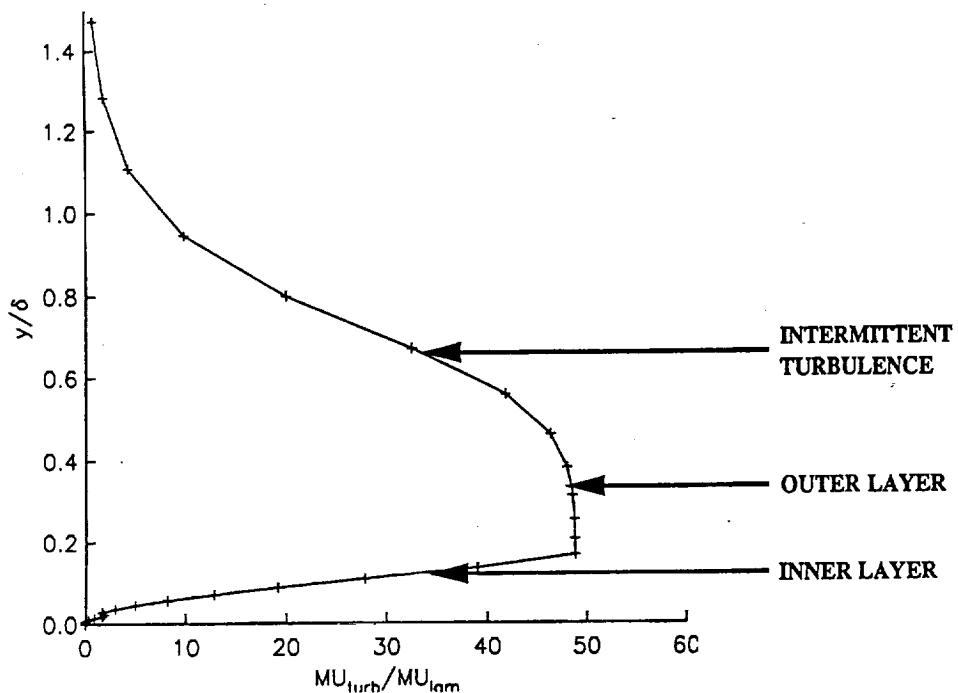
- EULER OR NAVIER-STOKES ANALYSIS
FOR STEADY 3-D FLOWS IN TURBOMACHINERY

FEATURES

- CARTESIAN FORMULATION, ROTATION ABOUT X-AXIS
RECTANGULAR OR ANNULAR GEOMETRIES
- SOLVES NAVIER-STOKES EQUATIONS
THIN-LAYER FORMULATION, (NO STREAMWISE VISCOUS TERMS)
RETAINS HUB-TO-TIP & BLADE-TO-BLADE VISCOUS TERMS
BALDWIN-LOMAX OR CEBECI-SMITH TURBULENCE MODEL
SIMPLE TIP CLEARANCE MODEL
- NODE-CENTERED FINITE-DIFFERENCE FORMULATION
EXPLICIT 4-STAGE RUNGE-KUTTA TIME-MARCHING SCHEME
2ND + 4TH ORDER ARTIFICIAL VISCOSITY, EIGENVALUE SCALING
VARIABLE $\Delta t_{i,j}$ & IMPLICIT RESIDUAL SMOOTHING
HIGHLY VECTORIZED & AUTOTASKED FOR CRAY Y-MP
- STACKED C-TYPE GRIDS



TURBULENT VISCOSITY PROFILE



CEBECI-SMITH & BALDWIN-LOMAX MODELS

INNER LAYER: PRANDTL-VAN DRIEST FORMULATION

CEBECI-SMITH

$$\begin{aligned}\mu_i &= \rho l^2 |\partial u / \partial y| \\ l &= \kappa y D \\ D &= 1 - \exp(-y^+ / A^+) \quad \text{VAN DRIEST DAMPING}\end{aligned}$$

BALDWIN-LOMAX

$$\mu_i = \rho l^2 |\omega|$$

OUTER LAYER: CLAUSER FORMULATION

CEBECI-SMITH

$$\begin{aligned}\mu_o &= K \rho \gamma \delta^* u_e \\ \gamma &= \left[1 + 5.5 \left(\frac{y}{\delta} \right)^6 \right]^{-1} \quad \text{KLEBANOFF INTERMITTENCY FUNCTION}\end{aligned}$$

BALDWIN-LOMAX

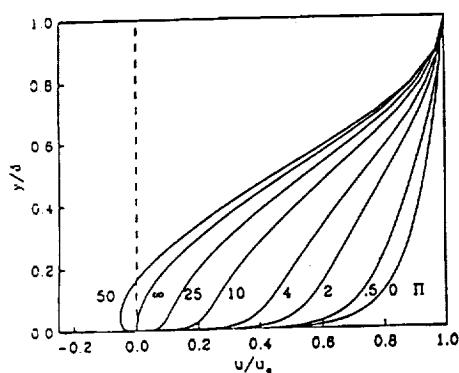
$$\mu_o = K \rho \gamma C_{cp} \min \left\{ \frac{y_{max} f_{max}}{\text{wake option}} \right\}$$

$$f(y) = y |\omega| D$$

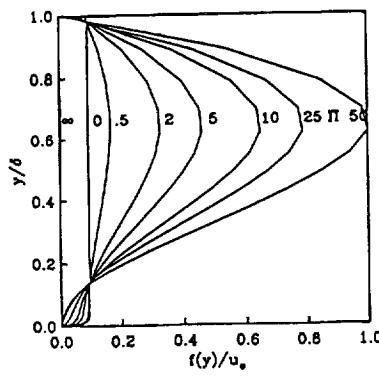
BALDWIN-LOMAX MODEL ANALYSIS

(SEE PAPER FOR DETAILS)

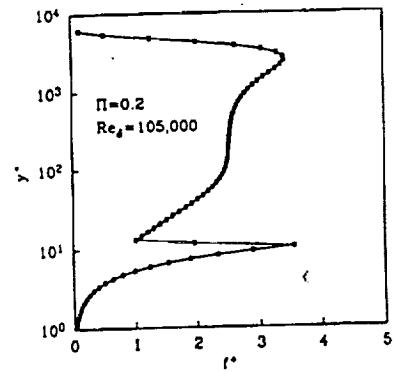
1. ASSUME SUBLAYER-WALL-WAKE VELOCITY PROFILE
2. CALCULATE BALDWIN-LOMAX FUNCTION $f(y)$
MAX. OCCURS AT $y_{max} = .646\delta$
INDEPENDENT OF PRESSURE GRADIENT
NO MAX. FOR INFINITELY FAVORABLE $\partial p / \partial x$
3. SPURIOUS MAX. CAN OCCUR AT EDGE OF VISCOUS SUBLAYER
MOST LIKELY AT LOW Re & FAVORABLE $\partial p / \partial x$



1. VELOCITY PROFILES, $Re_s = 105,000$



2. B-L FUNCTION $f(y)$



3. SPURIOUS MAXIMUM IN $f(y)$

PROPOSED TURBULENCE MODEL

INNER LAYER (SIMILAR TO BALDWIN-LOMAX)

$$\mu_i = \rho l^2 |\omega|$$

$$l = \kappa y D$$

$$D = 1 - \exp(-y^+ / A^+)$$

$$y^+ = y \frac{u^*}{\nu}$$

$$u^* = \sqrt{\frac{\tau_{wall}}{\rho}}$$

PROPOSED TURBULENCE MODEL

PRESSURE GRADIENT EFFECTS

- ACCELERATING FLOWS TEND TO RELAMINARIZE
- MODELLED BY INCREASING A^+ IN FAVORABLE $\partial p/\partial s$
- CEBECI'S EXPRESSION FOR A^+ USED:

$$A^+ = \frac{26}{\sqrt{1 + 11.8p^+}}$$

$$p^+ = \frac{\nu}{\rho u^{*3}} \frac{\partial p}{\partial s}$$

- PRESSURE GRADIENT EVALUATED USING:

$$\frac{\partial p}{\partial s} \approx \frac{\vec{V}_e}{|\vec{V}_e|} \cdot \nabla p$$

- "EDGE VELOCITY" \vec{V}_e EVALUATED AT A GRID LINE FAR ENOUGH FROM THE WALL TO GIVE THE GENERAL FLOW DIRECTION
- KAYS-MOFFATT EXPRESSION WAS TESTED, EFFECTS TOO STRONG

PROPOSED TURBULENCE MODEL

LOCAL SHEAR MODEL

- IN STRONGLY ACCELERATING FLOWS τ^+ DECREASES WITH y^+
- MODELLED BY REPLACING τ_{wall} WITH $\tau(y)$ IN D

$$D = 1 - \exp(-y^+/A^+)$$

$$y^+ = y \sqrt{\frac{\rho(\mu_l + \mu_t)}{\mu_l} |\omega|}$$

- ERROR IN ORIGINAL PAPER - USED $\mu_l |\omega|$ ONLY
- USED BY KAYS, PATANKAR-SPALDING, OTHERS
- ALSO USED TO AVOID PROBLEMS AT SEPARATION WHEN $\tau_{wall} \rightarrow 0$

PROPOSED TURBULENCE MODEL

OUTER LAYER

$$\begin{aligned}\mu_o &= K \rho \gamma \min \left\{ \frac{F}{C_{wk} \bar{y} (|V_{max}| - |V_{min}|)}, \right. \\ \gamma &= \left[1 + 5.5 \left(\frac{C_{Kleb} y}{\bar{y}} \right)^6 \right]^{-1} \\ C_{wk} &= 0.825 \\ C_{Kleb} &= 0.55\end{aligned}$$

PROPOSED TURBULENCE MODEL

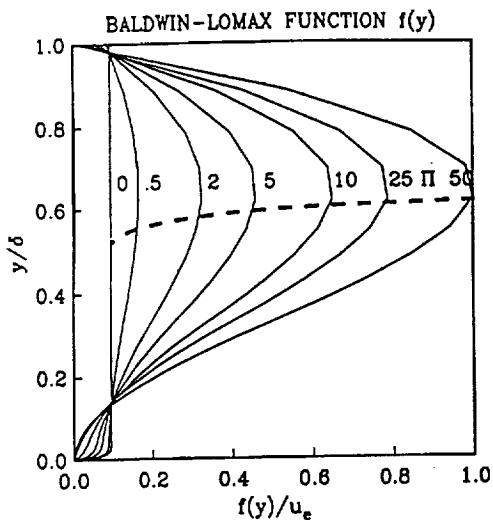
OUTER LAYER - FUNCTION F

- DEFINE $F = \int f dy$
- INTEGRATE BY PARTS ASSUMING $|\omega| \rightarrow 0$ AS $y \rightarrow \delta$

$$\begin{aligned}F &= \int_0^\infty y |\omega| dy \\ &\approx \int_0^\delta y \frac{\partial u}{\partial y} dy \\ &= uy|_0^\delta - \int_0^\delta u dy \\ &= \int_0^\delta (u_e - u) dy \\ F &= \delta^* u_e\end{aligned}$$

- USE F DIRECTLY IN CEBECI-SMITH OUTER FORMULATION
- ELIMINATES CONSTANT C_{cp}
- DOES NOT REQUIRE KNOWLEDGE OF δ OR u_e
- DISCOVERED INDEPENDENTLY BY D. A. JOHNSON, AIAA 92-0026

PROPOSED TURBULENCE MODEL



OUTER LAYER - LENGTH SCALE \bar{y}

- \bar{y} IS THE CENTROID OF THE $f(y)$ CURVE

$$\int_0^{\bar{y}} f(y) dy = \int_{\bar{y}}^{\delta} f(y) dy$$

- EVALUATE USING COLE'S VELOCITY PROFILES

$$\Pi \quad \bar{y}/\delta$$

$$0 \quad .5$$

$$.5 \quad .55$$

$$\infty \quad .606$$

- USE EQUILIBRIUM VALUE $C_{Kleb} = \bar{y}/\delta = .55$

PROPOSED TURBULENCE MODEL

OUTER LAYER - WAKE MODEL

$$\mu_o = K \rho \gamma \min \left\{ \frac{F}{C_{wk} \bar{y} (|V_{max}| - |V_{min}|)} \right\}$$

- LOWER OPTION IS A CONVENTIONAL WAKE MODEL
- EVALUATE C_{wk} BY EQUATING TWO OPTIONS, ASSUMING

$$\bar{y}_{sep} = .606 \delta$$

$$F_{sep} = u_e \delta / 2$$

$$\Delta V / u_e \approx 1$$

- GIVES $C_{wk} = 0.825$

PROPOSED TURBULENCE MODEL

3-D IMPLEMENTATION

- GRANVILLE BLENDING FUNCTION

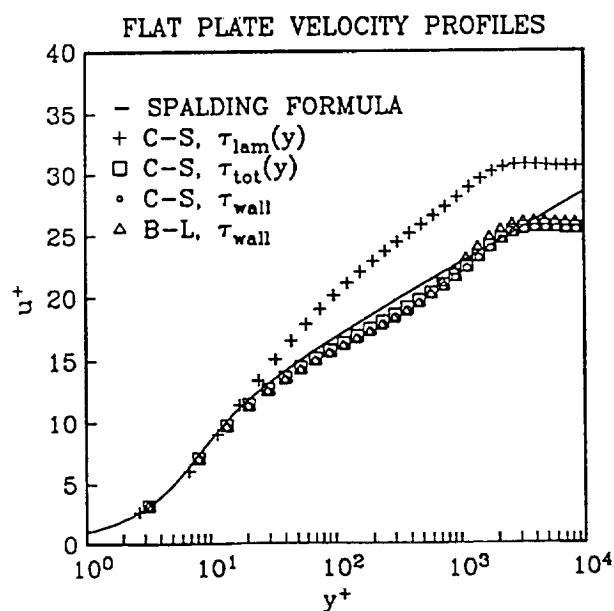
$$\mu_{eff} = \mu_o \tanh \frac{\mu_i}{\mu_o}$$

- MODEL APPLIED INDEPENDENTLY IN BLADE-TO-BLADE (η) AND SPANWISE (ζ) DIRECTIONS
- INNER LAYER - USE BULEEV LENGTH SCALE

$$y_i = \frac{2s_\eta s_\zeta}{s_\eta + s_\zeta + \sqrt{s_\eta^2 + s_\zeta^2}}$$

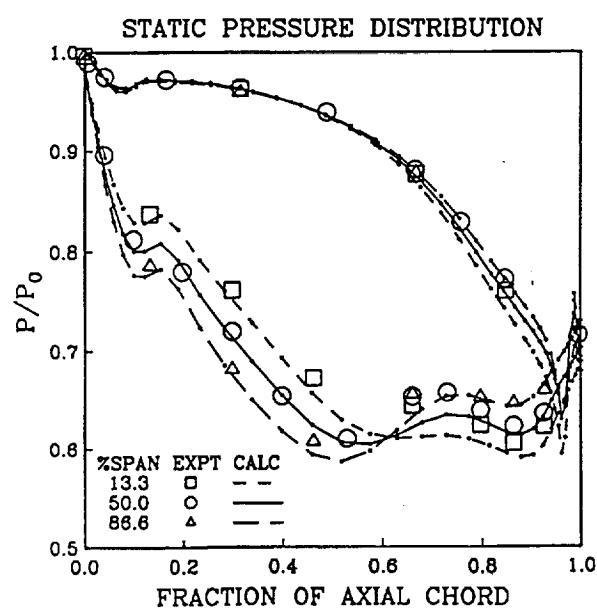
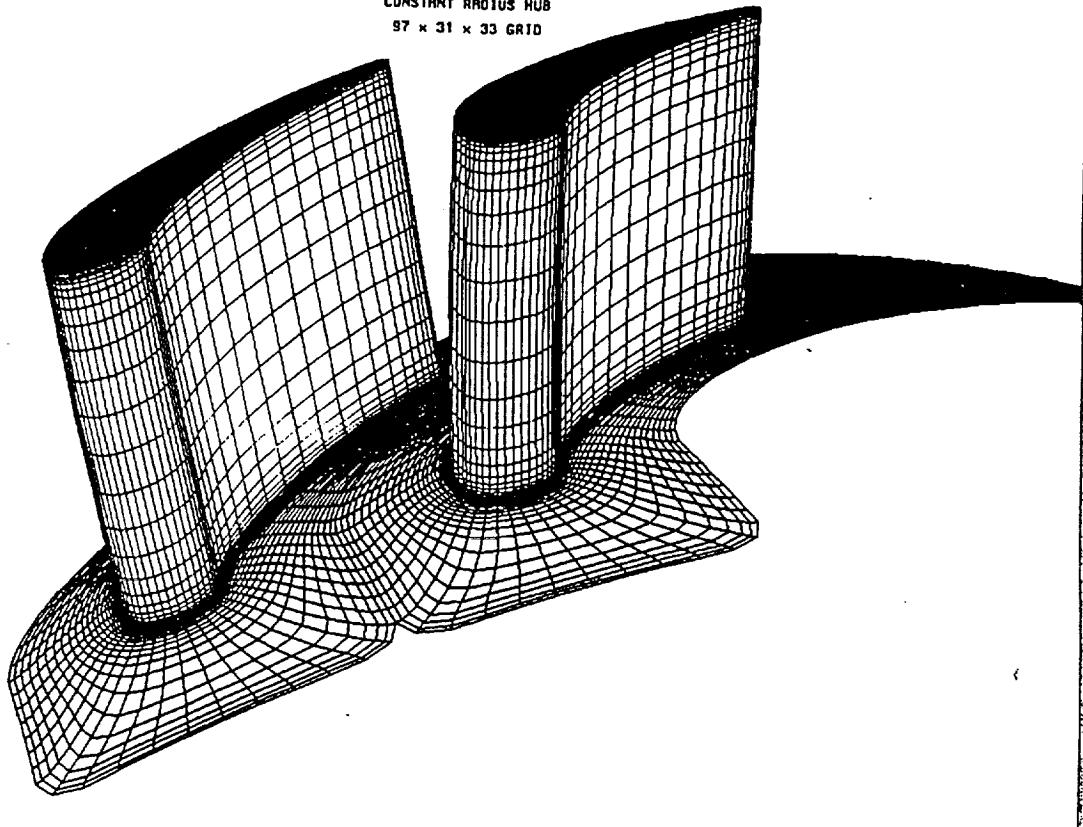
- OUTER LAYER - USE ACTUAL DISTANCE ACROSS PROFILE
- BLEND η AND ζ PROFILES VECTORALLY

$$\mu_{turb} = \sqrt{\mu_{i\eta}^2 + \mu_{i\zeta}^2}$$

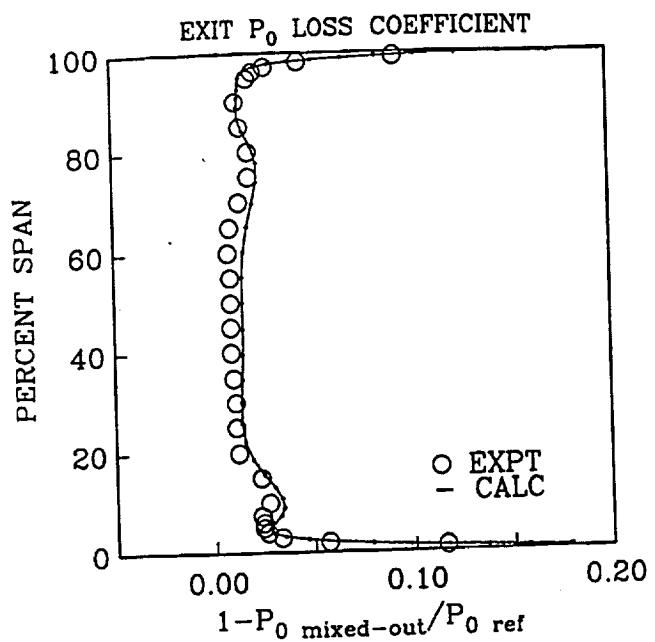


COMPARISON OF FLAT PLATE VELOCITY PROFILES
TO SPALDING'S COMPOSITE LAW OF THE WALL

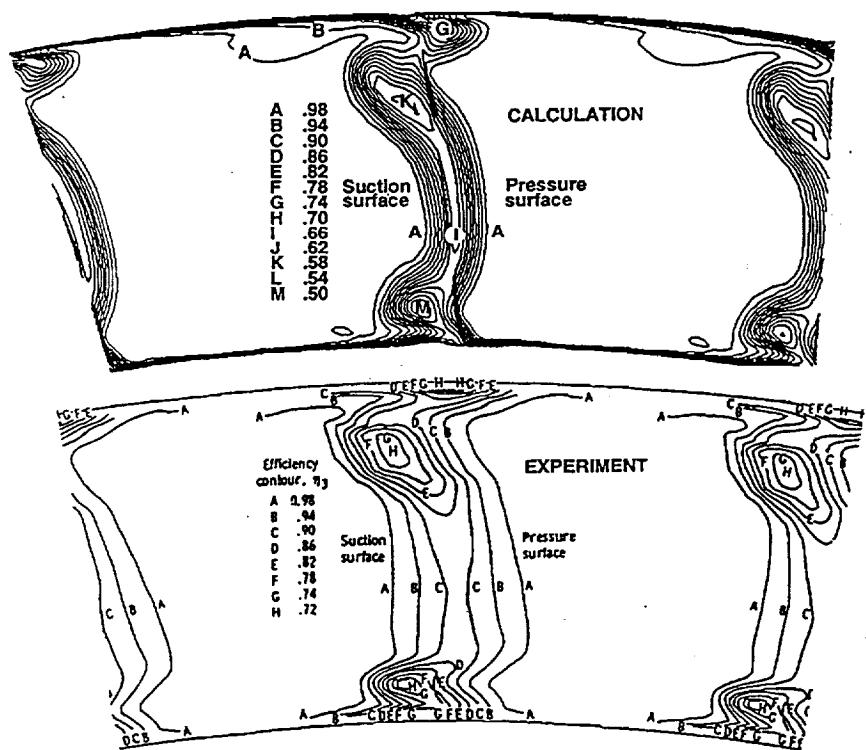
GOLDMANS ANNULAR CASCADE
CONSTANT RADIUS HUB
97 x 31 x 33 GRID



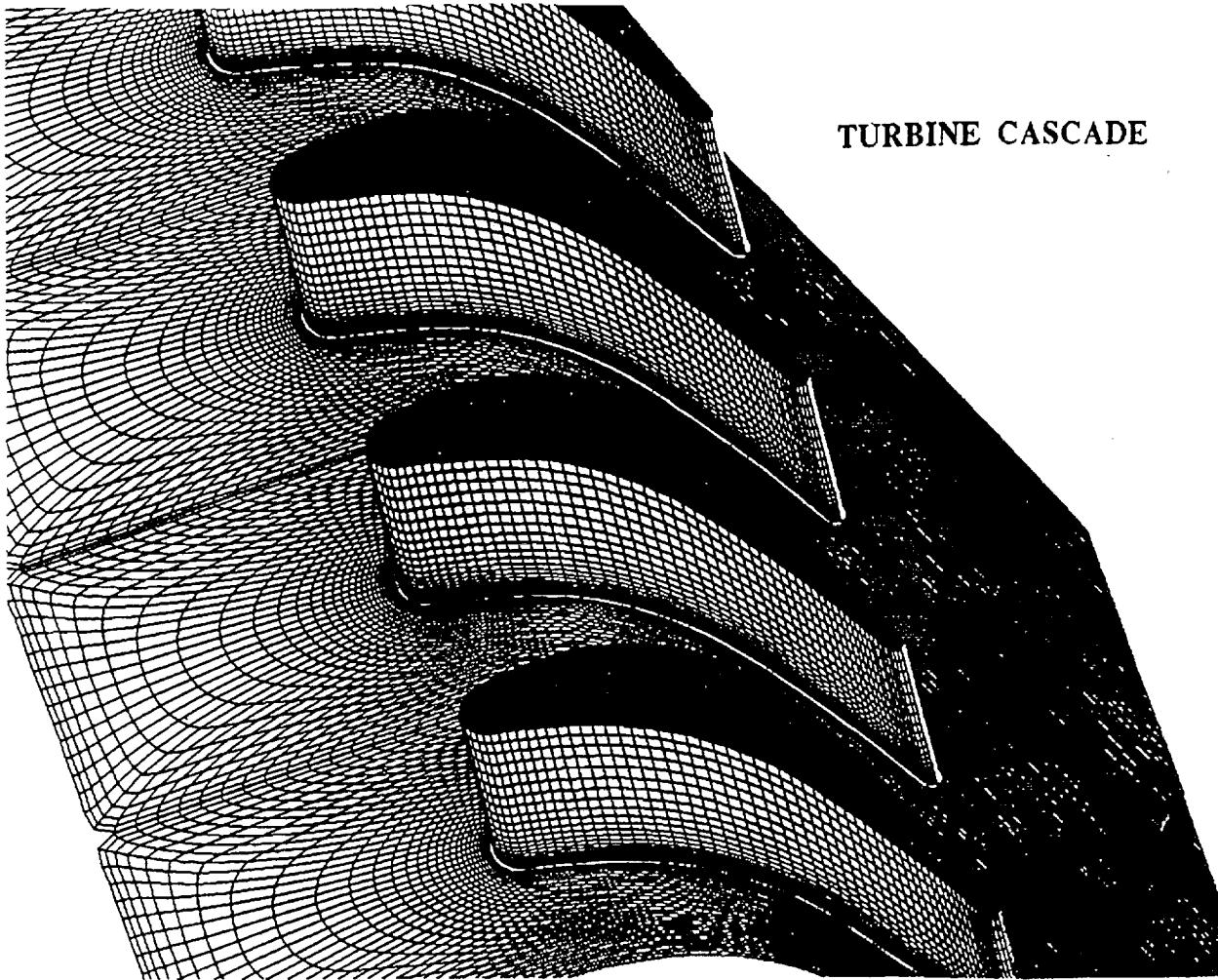
COMPUTED & MEASURED PRESSURE DISTRIBUTIONS
FOR THE ANNULAR TURBINE CASCADE



COMPUTED & MEASURED LOSS COEFFICIENT PROFILES
FOR THE ANNULAR TURBINE CASCADE

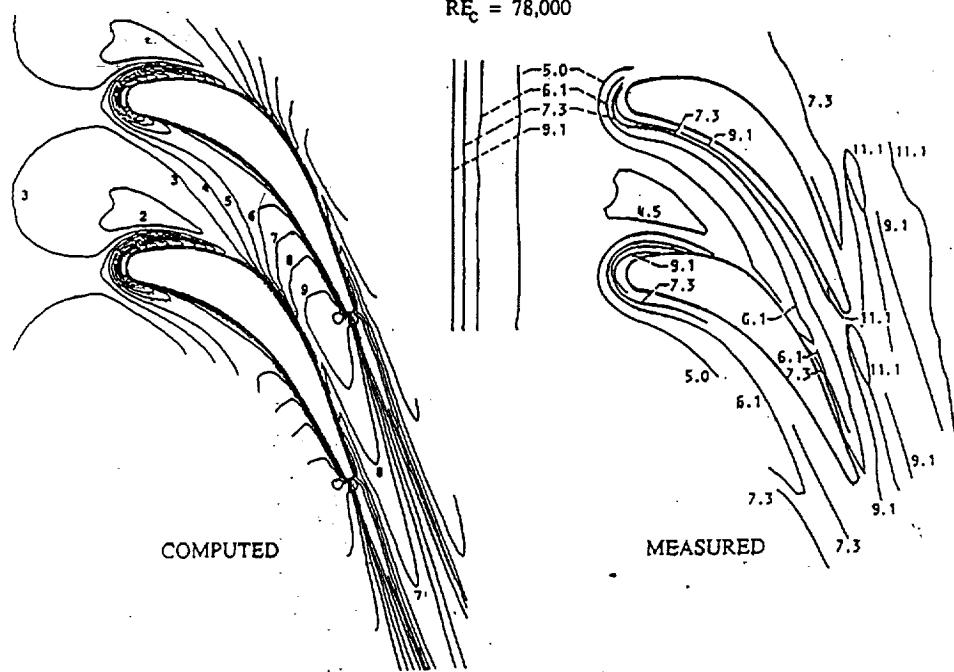


COMPUTED & MEASURED EFFICIENCY CONTOURS
IN THE WAKE OF THE ANNULAR TURBINE CASCADE

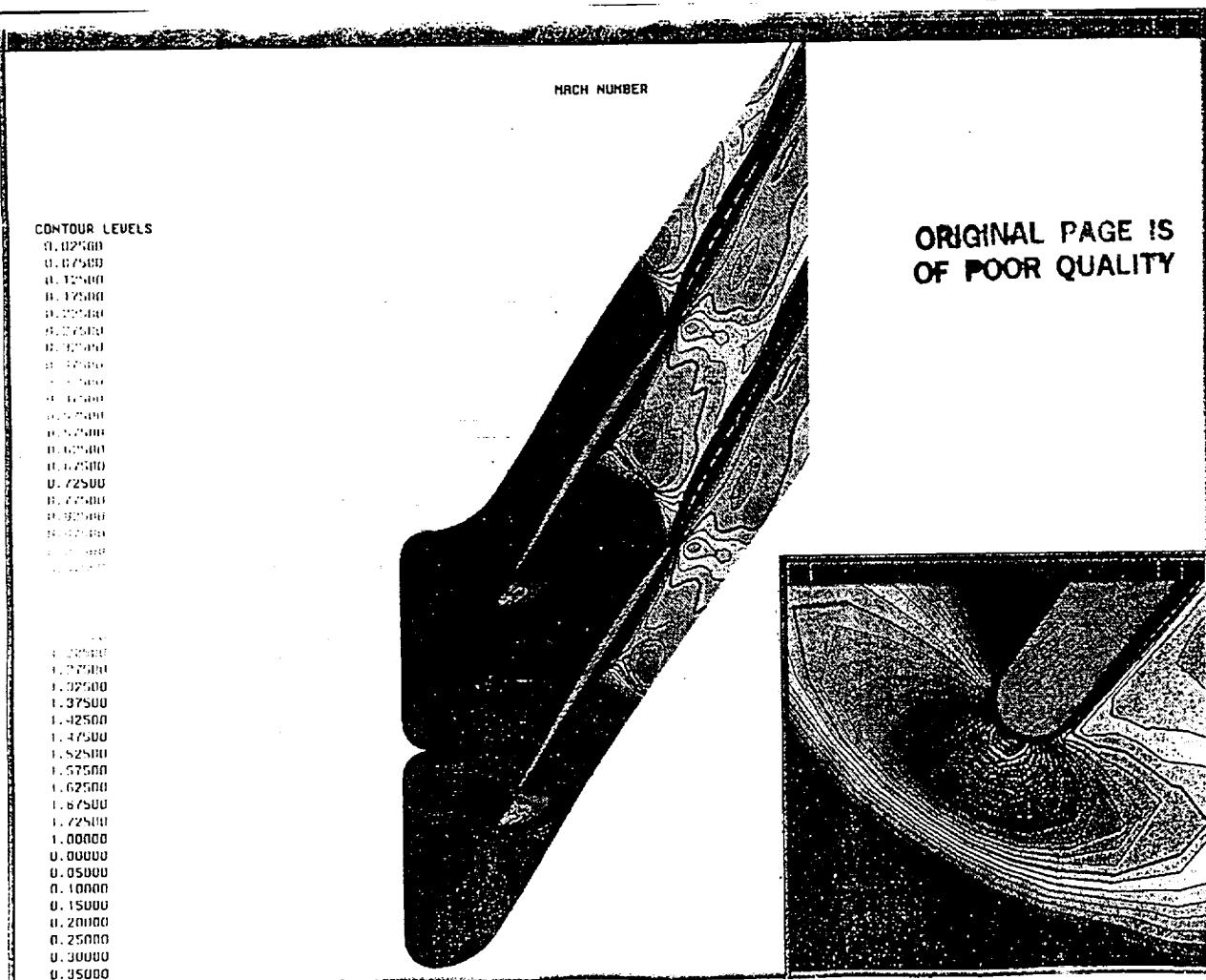
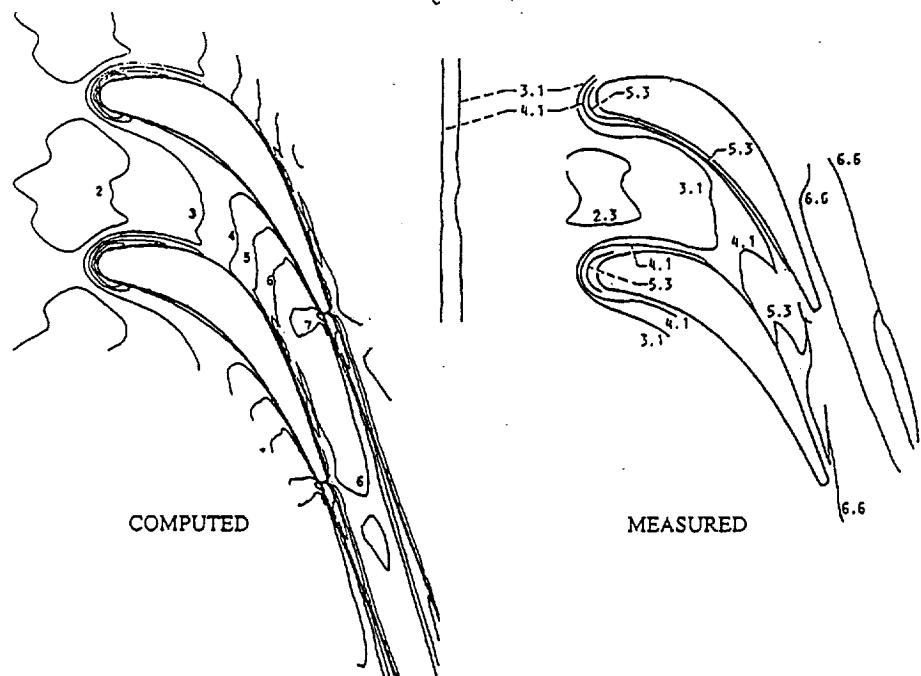


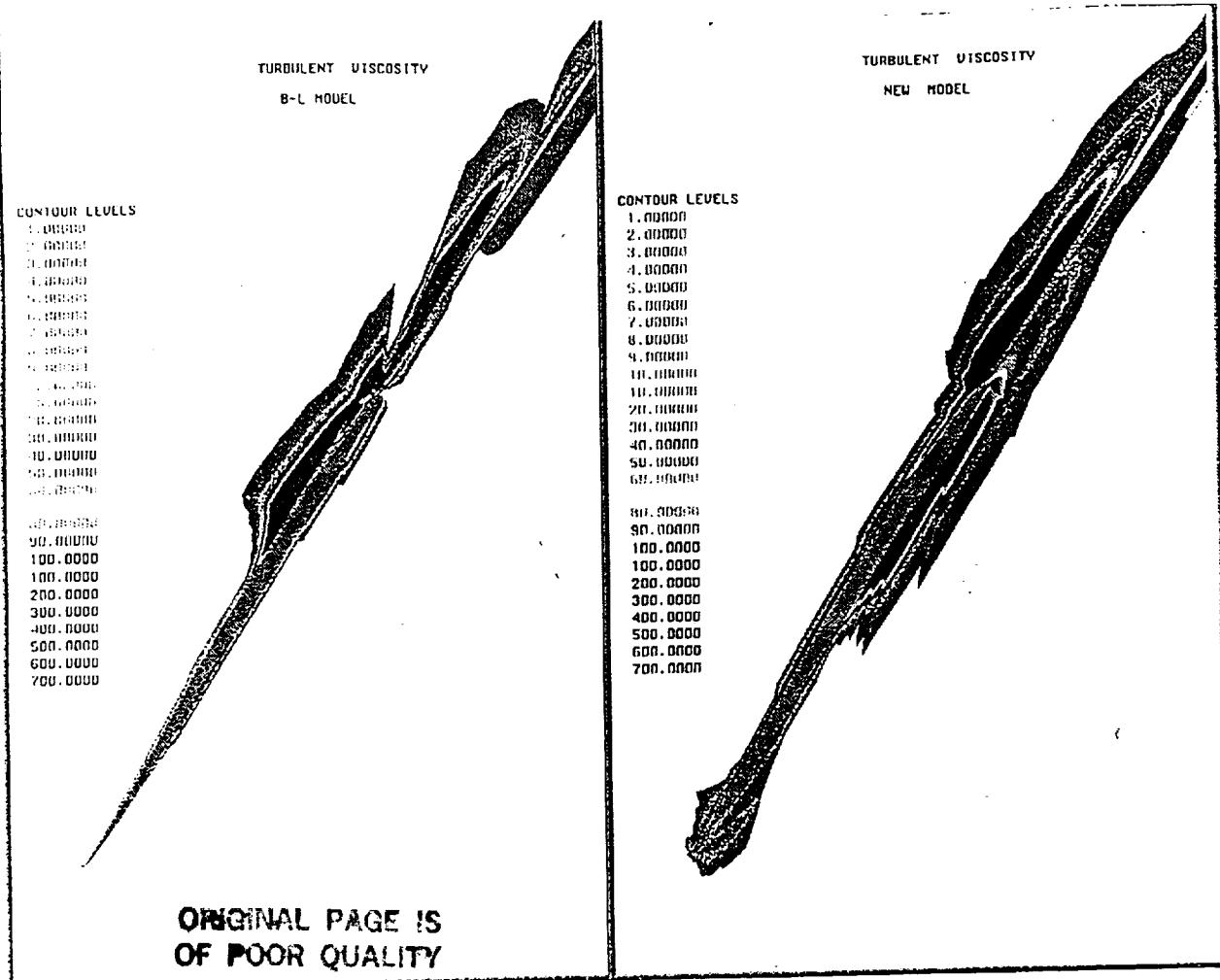
TURBINE CASCADE

BOYLE'S LINEAR CASCADE
STANTON NUMBER $\times 1000$
 $RE_c = 78,000$



BOYLE'S LINEAR CASCADE
STANTON NUMBER $\times 1000$
 $RE_c = 490,000$





SUMMARY

- SPURIOUS MAXIMUM IN B-L FUNCTION $f(y)$ CAN GIVE INCORRECT TURBULENT LENGTH SCALE & ERRATIC ST OR C_f PATTERNS
 - MOST LIKELY AT LOW Re AND FAVORABLE $\partial p/\partial s$
- NEW TURBULENCE MODEL PROPOSED
 - INTEGRAL RELATIONS FOR $\delta^* u_c$ AND δ USED WITH C-S MODEL
 - EFFECTS OF $\partial p/\partial s$ MODELED
 - WAKE MODEL PROPOSED
- FLAT PLATE
 - B-L & NEW MODEL AGREE WITH LAW OF THE WALL
 - LOCAL SHEAR MOD. DOES NOT AGREE WITH LAW OF THE WALL
- ANNULAR TURBINE
 - GOOD AGREEMENT WITH EXPT. PRESSURE DISTRIBUTION
 - WAKE MIXING UNDER-PREDICTED
- TURBINE ENDWALL HEAT TRANSFER
 - VARIATIONS IN ENDWALL ST WITH Re PREDICTED WELL
 - EFFECTS OF $\partial p/\partial s$ IMPORTANT
- TRANSONIC FAN
 - SHEAR LAYER FROM BOW SHOCK ACTS LIKE VISCOS LAYER
 - NEW MODEL OVERPREDICTS L.E. μ_t
 - B-L MODEL PREDICTS REASONABLE L.E. μ_t